

We pitch from a local minimum vertex (the time coordinate of the vertex is minimum relative to its star)

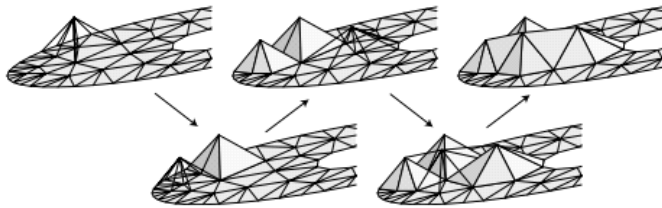
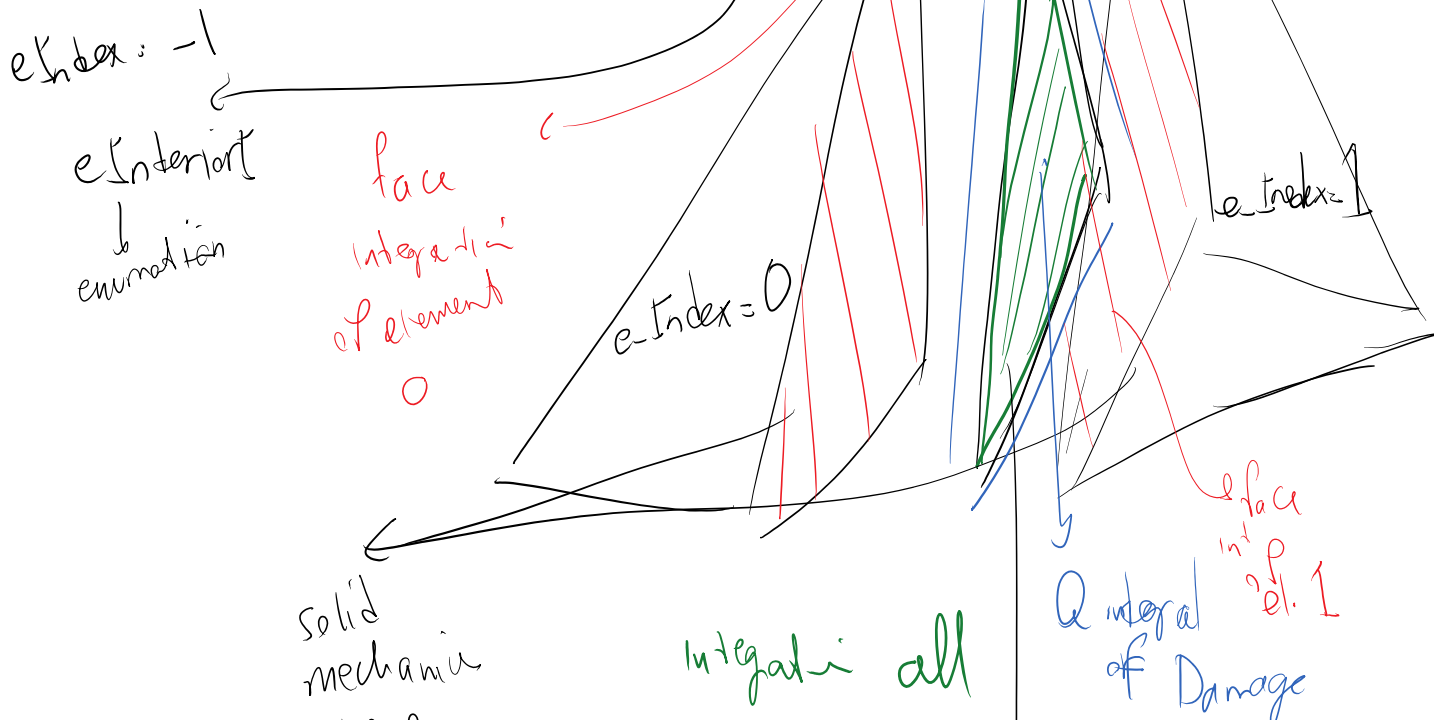


Fig. 4. Pitching tents in space-time.



solid mechanics here

Integrating all of Damage  
 ↓  
 Damage model here

Damage model weighted residual

$$\int_{\Omega} \hat{D} (\dot{D} - D_{src}) dv + \int_{\partial a} \hat{D} (D^* - D) n_i ds = 0$$

Interior of

Solid Mechanics

PIC (Physics Integrating Cell)

$$\int_{\Omega} (\hat{u} p + \nabla \hat{u} \cdot \sigma + \hat{u} \rho b) dv +$$

$$\int_{\partial a} \hat{u} \sigma^* n_i ds - \hat{u} p n_i ds + [E] \hat{\sigma} n_i ds + [\hat{u}] \delta n_i ds$$

$$+ \hat{u}_0 [u] n_i ds = 0$$

$p = \rho v = \rho \dot{u}$  linear momentum  $v = \dot{u}$  velocity

$E = \frac{1}{2} (\nabla u + \nabla u^T)$  strain  $\sigma = C^T E$  stress

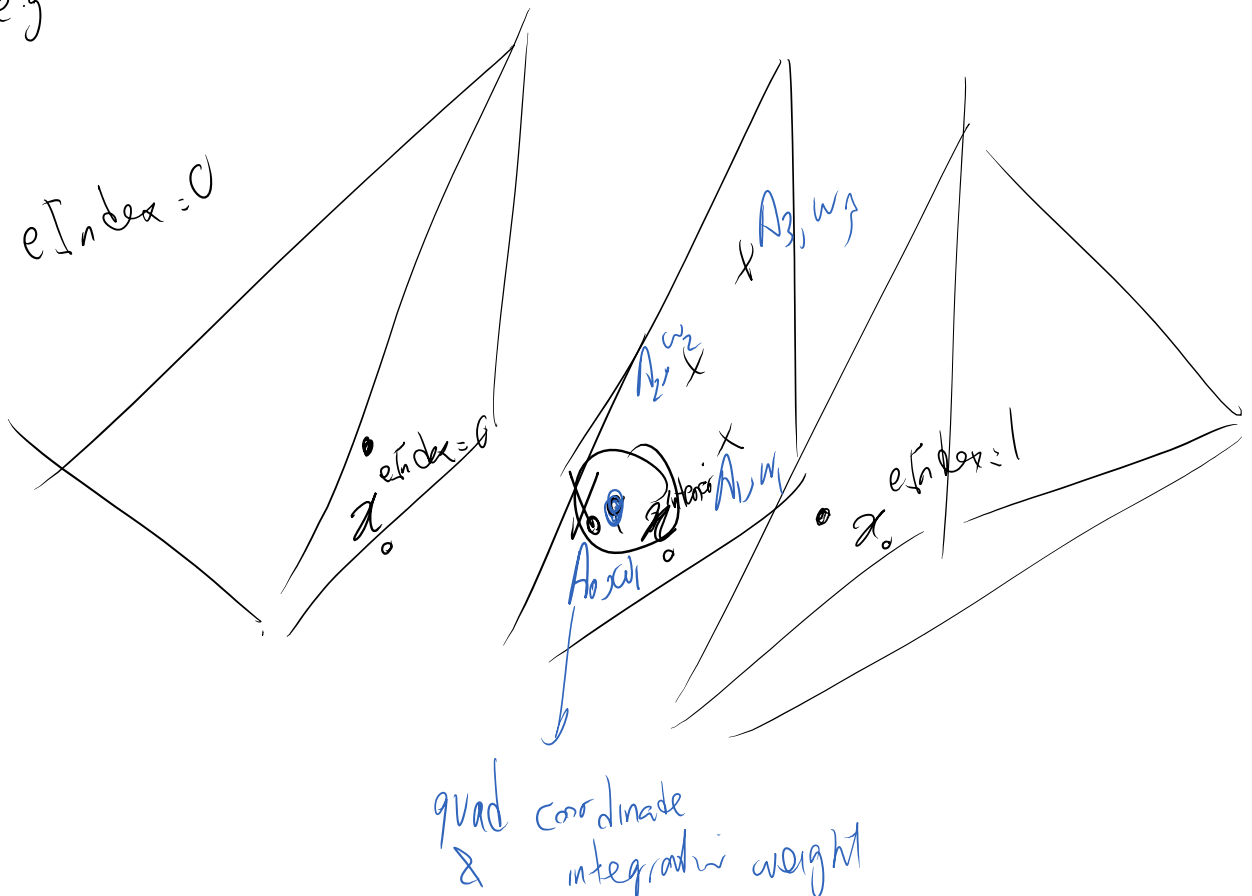
$$[f] := f^* - f$$

$\vec{n}_x, n_t$  are spatial & temporal normals to a face

The process for the solution of integration cell:

1. Set the integration order: for all the elements attached to PIC we ask them to give their integration order for the given type of cell integration.
2. From integration order  $\rightarrow$  integration points and weights

e.g. order = 5



3. Loop over the quadrature points

3.1 Form Coord

- 1 - Quadrature coordinate      Alpha (A)
- 2 - Global coordinate          X
- 3 - basis coordinates

physics\PhyCoord.h

class ptCoords

*Interior basis coordinate*

eCoord eCrdInterior;      // the coordinate for element on interiorIntegration cell  
vector<eCoord> eCrdFacet;      // the vector of coordinates for elements on facetIntegration cells  
*facet basis coordinate*

// storing integration related members:

// actual position of point

QCoord quadC;      // quadrature coordinate for integration cell

*Alpha*

XCoord XC;      // global cartesian coordinate

X

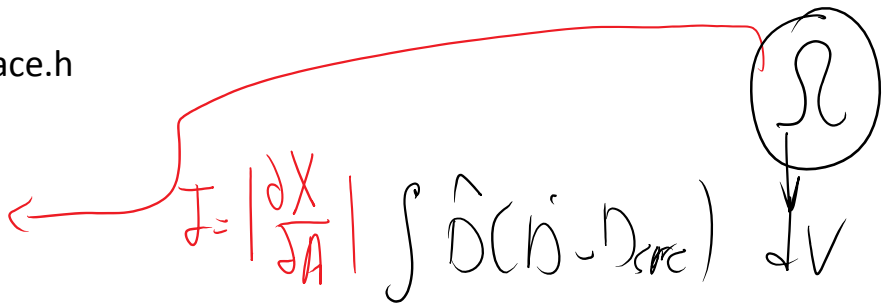
Last member of the coordinate:

GeomPropInt\* gpi;

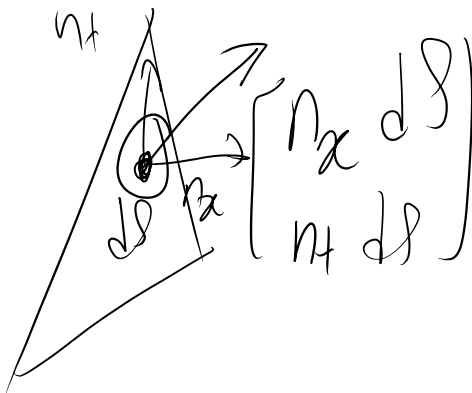
physics\PhyGeomInterface.h  
 class GeomPropInt

double omega2Alpha;

vector<PhyFacetForms> facet\_dForms;



for faces



$$M = p - \sigma$$

$$= p v \underbrace{ndt}_{n_t dS} - (C \epsilon) \underbrace{ndx}_{n_x dS}$$

The class Facet forms:

physics\PhyFacetForms.h

class PhyFacetForms

...  
 VECTOR sdxAll;

like SPACETIME normal  
 \* dS

Often `GeomPropInt` doesn't change much and basically for constant Jacobian PIC it's constant.

Trick:

We create a `ptCoords` (coordinate) at integration cell at the centroid and set it up IF the PIC is constant Jacobian. Then for any point if the element is constant Jacobian we just borrow precomputed properties from the centroid. Otherwise, we calculate it per-point.

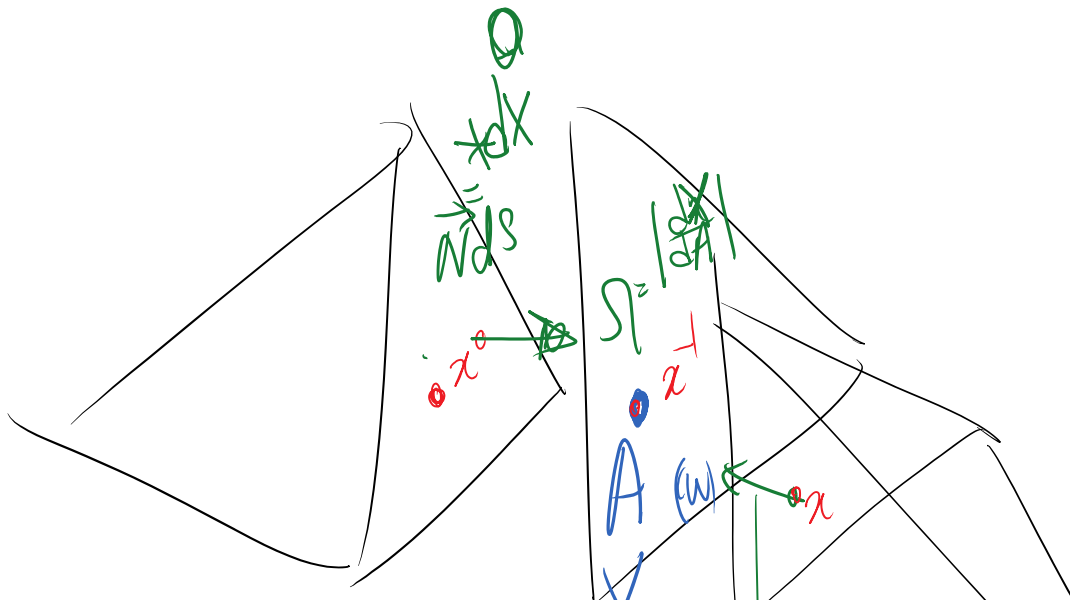
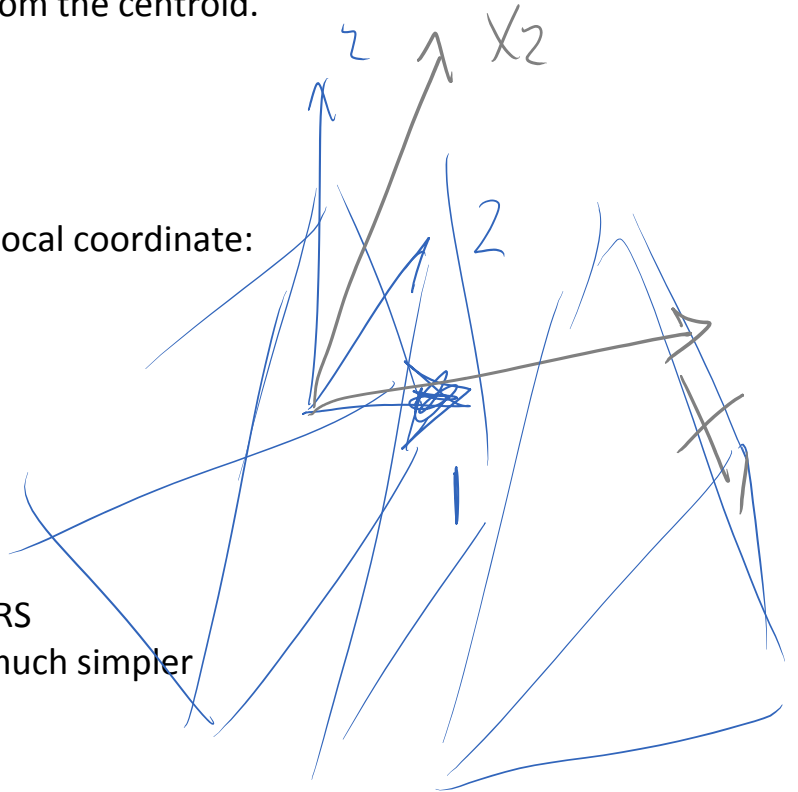
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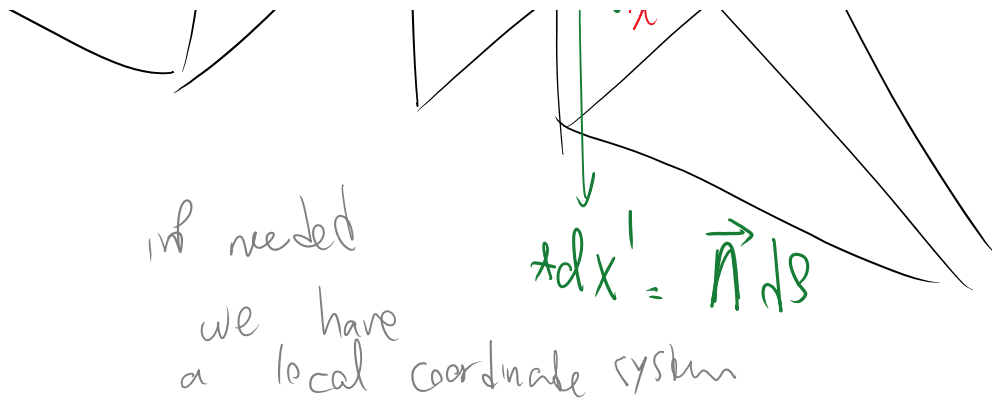
The last member of `GeomPropInt` is a local coordinate:

```
bool hasLocalCoord;
V2TENSOR localCoordBasis; }
```

Benefits of a local coordinate:

1. Many terms become zero in the WRS
2. Target value calculation becomes much simpler





$$\int_Q \hat{D} (\dot{D} - D_{src}) dv + \int_{\partial Q} \hat{D} (D^* - D) n_t ds = 0$$

$$\int_Q (\hat{u} p + \nabla \hat{u} \cdot \sigma + \hat{u} p b) dv +$$

$$\int_{\partial Q} \hat{u} \sigma n_x ds - \hat{u} p n_t + [E] \sigma n_t ds + [\hat{u}] \delta n_x ds + \hat{u}_e [u] ds = 0$$

Naming tensor fields

Tensor fields are recognized by their physics type and computation type

```

class PhyFldC
phyFld phyF;
compT cT;

```

→ physics name (stress, disp. strain, ...)
   
 → value, DT, DX, symDX, Div, Src, \*

	U	V	E	$\sigma$	$\rho$	D	-	.
value								
( <sup>o</sup> )								
$\nabla$								
Div								
*								

Each of the elements (interior and faces) require their storage for values.

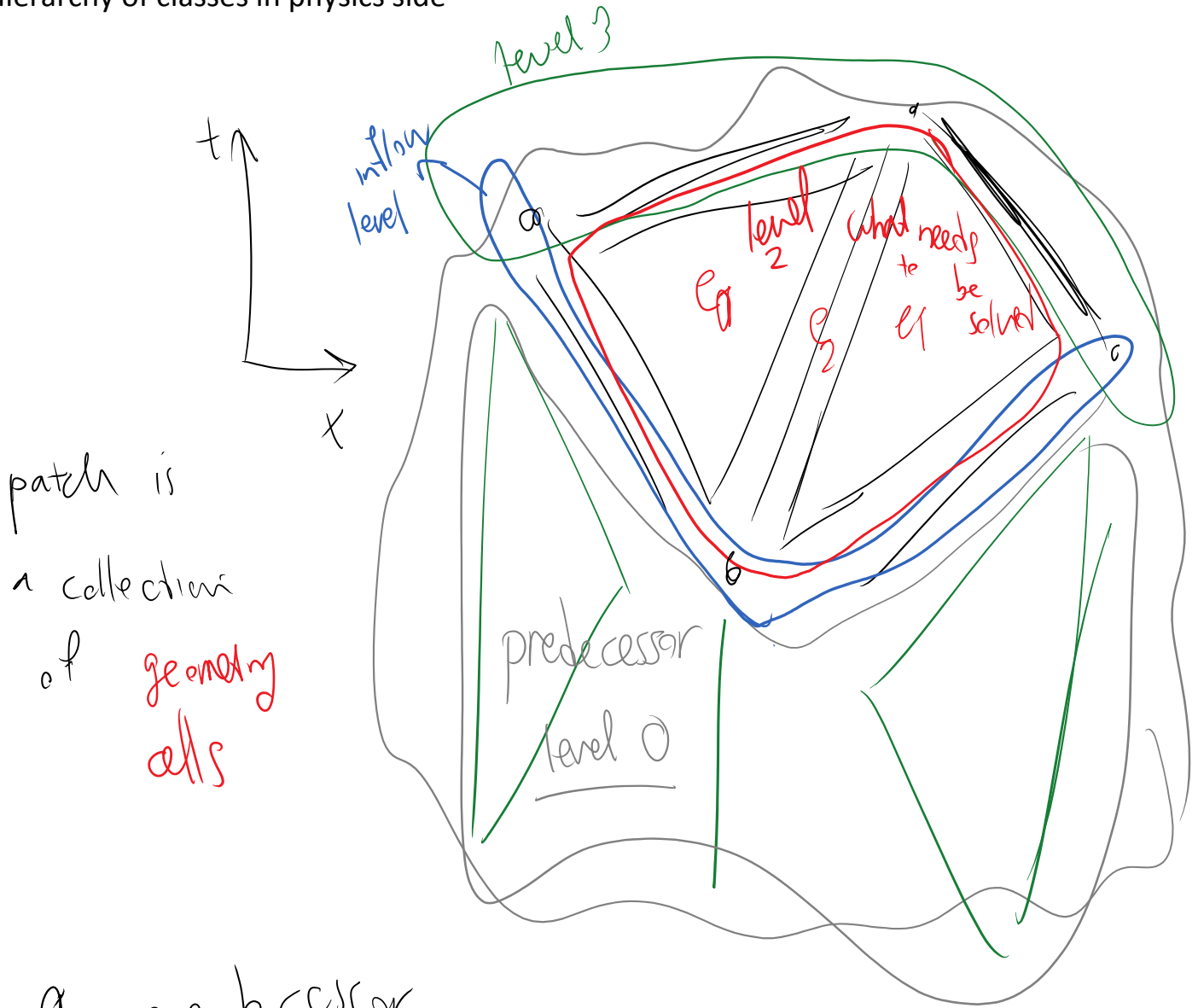
To be continued next time

Hierarchy of classes in physics side

novel 3



# Hierarchy of classes in physics side



0 - predecessor

1 - inflow

2 - active

3 - outflow

new elements

patch  
↓

< phy Elements >

$e_0, e_1, e_2$

↓  
< faces > (intervals)

< physics >

[Solid, thermal, - -]

↓  
vector (tensor fields)

