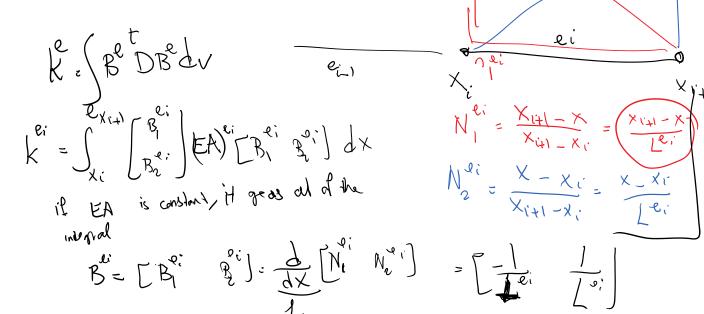
the local by assembled to global For matches contributions of element e

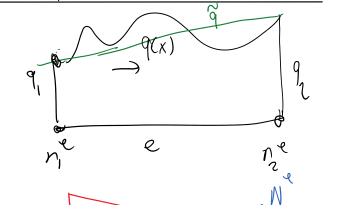
There were two other formulas I used last time:

1. Element stiffness matrix



$$\frac{2nd}{fr} = \int_{N_z}^{R_z} q(x) dx = \int_{N_z}^{R_z} q(x) dx$$

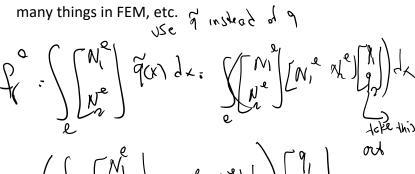
$$= \int_{N_z}^{R_z} q(x) dx = \int_{N_z}^{R_z} q(x) dx$$

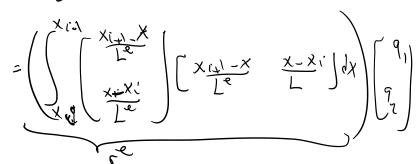


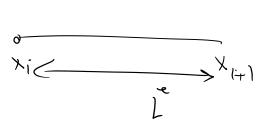
$$\frac{9(x)}{9(x)} = 9(1)(x) + 9(1)(x)$$

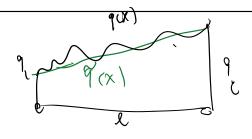
This function matches the end point values of q due to delta property of FE shape functions.

In fact, finite element shape functions are used to interpolate many things in FEM, etc.







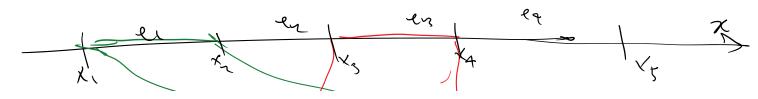


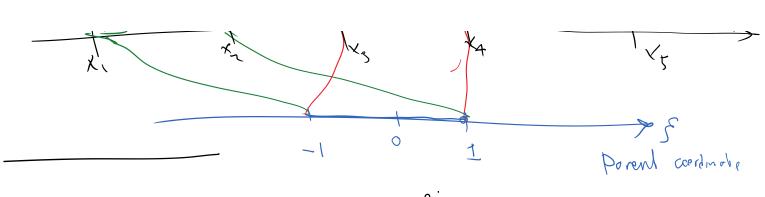
In FEM (and other numerical methods) we have discretization error (infinite unknowns to a finite number).

This introduces discretization error (FEM as Ch^2 for linear bar element).

As long as all the other errors go zero as fast or faster than discretization error, we are fine with them because eventually as h (element size) goes to zero, we converge to the exact solution

Last step to make all the elements be similar:





N, = a & + b

 $N_{1}(n_{1}) = 1$: $N_{1}(\xi = -1) = \alpha(-1) + b = 1$ $N_{1}(n_{2}) = 0$ $N_{2}(n_{2}) = 0$ $N_{3}(n_{2}) = 0$ $N_{4}(n_{2}) = 0$ $N_{5}(n_{2}) = 0$ $N_{5}(n_{2}$

Smilety Notes) = 1 + 15

Fronder Way

 $N_{1}(\xi) = \frac{(\xi - \xi_{2})}{(\xi_{1} - \xi_{1})} = \frac{\xi - 1}{7}$

 $N_{2}(s) = \frac{s-s_{1}}{s_{2}-s_{1}} \cdot \frac{s-s_{1}}{s-s_{1}} \cdot \frac{s-s_{1}}{s}$

Calcelate the stiffness matrix

K= JBtoBbv

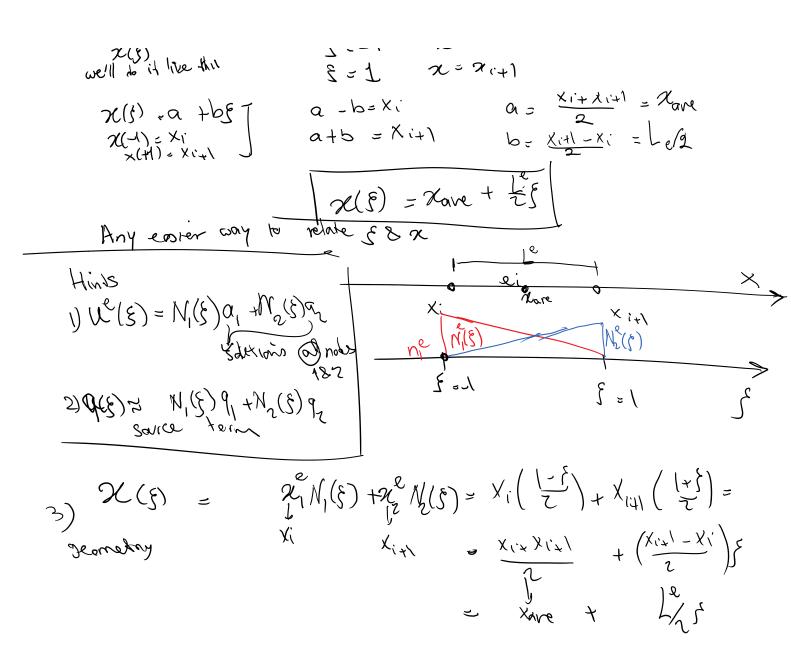
= (Xi+) [B] EA [B, B) dx

 $X_i = \frac{1}{3} \left[N_i N_i \right] , \text{ but } N_i(\S) = \frac{1}{3} \left[N_i = \frac{1+1}{3} \right]$

B= d/2 [1-5 (+5)

coeff to it like this

ξ=-\ χ=π: ξ=1 χ=π:+1



So, now we have a relation between x and \mathcal{E}

Go back to the formula for the stiffness matrix

Back to equation 1:

$$K = \begin{cases} B^{t} DB dV \\ E \\ E \end{cases}$$

$$= \begin{cases} Xi+1 \\ B_{1} \\ EA \end{cases} EA \begin{cases} B_{1} \\ B_{2} \end{bmatrix} dX$$

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$$B = \frac{1}{dx} N(f) = \frac{1}{dx} \frac{1}{dx}$$

$$B = \frac{1}{dx} N(f) = \frac{1}{dx} \frac{1}{dx}$$

$$\frac{X(f) : N_{out} + \frac{1}{c}f}{dx}$$

$$B = \frac{1}{dx} \frac{1}{dx} \frac{1}{dx}$$

$$B = \frac{1}{dx} \frac{1}{dx} \frac{1}{dx} \frac{1}{dx}$$

$$B = \frac{1}{dx} \frac{1}{dx} \frac{1}{dx} \frac{1}{dx}$$

$$Again equal in (1)$$

$$B = \frac{1}{dx} \frac{$$

TEN
Silfnos

$$k^2 = \frac{1}{2!^2} \left[-1 \right] \int_{1}^{1} EA(E) dE genund$$

The silfnos

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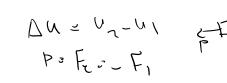
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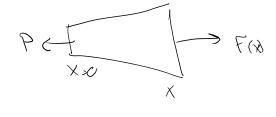
$$\mathcal{E}(X) = \frac{\partial u(X)}{\partial X} \longrightarrow \mathcal{U}(X_2) - \mathcal{U}(X_1) = \int_{X_1 = 0}^{x_2 + 1} \mathcal{E}(X) dX \qquad (i)$$

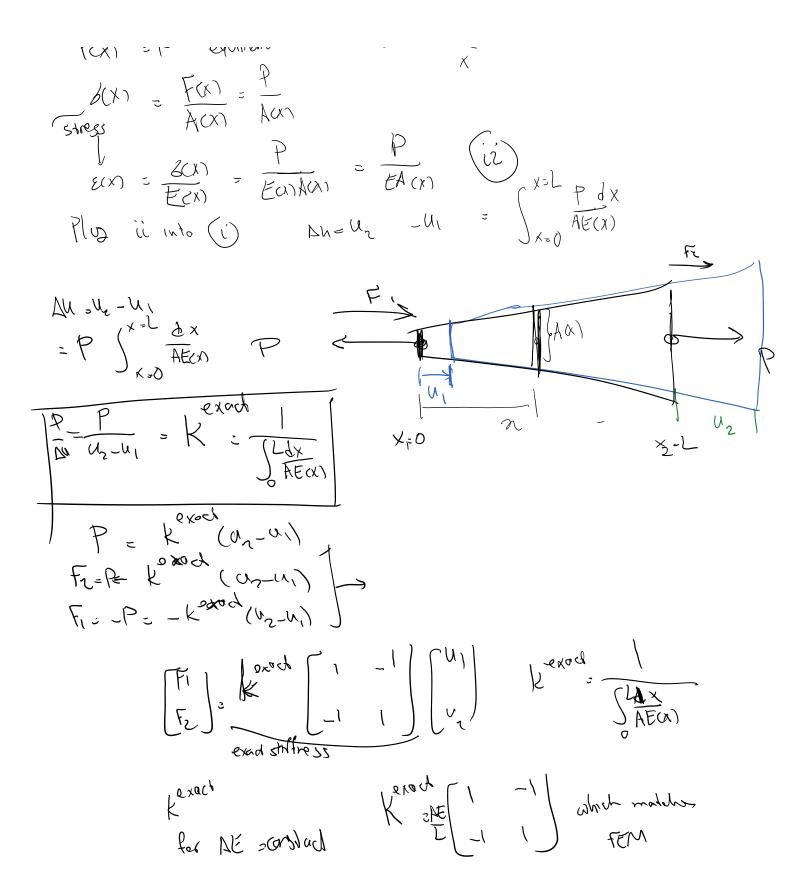
at position x

Force

FCXI = P equilibrium

2147





In your HW for an example, you'll realize that FEM give you a stiffer solution (stiffness). FEM is always stiffer than real solution