

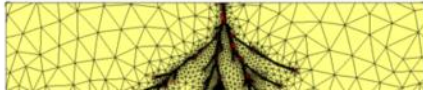
2020/08/19

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ME 517 – Finite Elements

ME 524 – Fracture Mechanics

Course webpage:

<http://rezaabedi.com/teaching/fracture-mechanics/>

Course syllabus can be access through the link above

http://www.rezaabedi.com/wp-content/uploads/Courses/FractureMechanics/SYLLABUS-FEM_524.pdf

This document has a more detailed overview of what will be covered in this course:

<http://www.rezaabedi.com/wp-content/uploads/Courses/FractureMechanics/TopicsDetails.pdf>

Fracture Mechanics Topics & References

Color Code: Covered, *Brief Discussion*, Not Covered

1. Preliminaries: Tensors; Kinematics (displacement, strain); Stress; Balance laws; Constitutive equations
Saouma 5.1-5.4; Anderson A2.1
2. History
Anderson 1.2.1-1.2.5
3. Fracture modes
 - 3.1. Classification
Murakami 1.1.1, 1.1.2, 1.1.3; Saouma 4.1-4.4 (buckling, fracture, yielding, etc.); Schreurs 2.1.
 - 3.2. Ductile fracture
 - 3.2.1. Dislocation dynamics
Hertzberg 2 (theory), 3 (slip and twinning)
 - 3.2.2. Void nucleation, growth, and coalescence
Anderson 5.1
 - 3.3. Brittle fracture
Anderson 5.2; Lawn
 - 3.4. Ductile-brittle transition
 - 3.4.1. Temperature
Anderson 5.3

Useful online courseware and links

1. Presentation on Fracture Mechanics by Dr. N. V. Phu from University of Adelaide. With special thanks to Dr. Phu, the majority of course presentations are based on Dr. Phu's presentations.
2. S. Suresh, Fracture and Fatigue, MITOpen courseware.
3. V.E. Saouma, Fracture Mechanics lecture notes, University of Colorado, Boulder.
4. P.J.G. Schreurs, Fracture Mechanics lecture notes, Eindhoven University of Technology (2012).
5. A.T. Zender, Fracture Mechanics lecture notes, Cornell University.
6. K. Ramesh, Engineering fracture mechanics lecture videos, IIT, Madras, India.
7. L. Zhigilei, MSE 2090: Introduction to the Science and Engineering of Materials, University of Virginia: Excellent lecture notes on material preliminaries such as atomic structure (ch2), crystalline solids (ch3), imperfections (ch4), mechanical properties (ch6), dislocation (ch7), and **failure (ch8)**.

Selected Bibliography

1. T. L. Anderson, *Fracture Mechanics: Fundamentals and Applications*, 3rd Edition, CRC Press, USA, 2004 (main textbook).
2. D. Broek, *Elementary Engineering Fracture Mechanics*, 4th Revised Edition, Springer, 1982 (or reprint 2013).
3. B. Broek, *The Practical Use of Fracture Mechanics*, Springer, 1998.
4. S. Murakami, *Continuum Damage Mechanics: A Continuum Mechanics Approach to the Analysis of*

5. S. Suresh, Fatigue of Materials, 2nd ed., Cambridge University Press, 1998.
6. L.B. Freund, Dynamic Fracture Mechanics, Cambridge University Press, 1998.
7. B. Lawn, Fracture of Brittle Solids, Cambridge University Press, 1993.
8. M.F. Kanninen and C.H. Popelar, Advanced Fracture Mechanics, Oxford Press, 1985.
9. R.W. Hertzberg, Deformation and Fracture Mechanics of Engineering Materials, 5th ed., John Wiley & Sons, Inc., 2012 (material focus).
10. S. Al Laham, Stress Intensity Factor and Limit Load Handbook, British Energy Generation Limited, 1998.
11. H. Tada, P.C. Paris, G.R. Irwin, Stress Analysis of Cracks Handbook, 3rd ed., ASME Press, 2000

<http://www.rezaabedi.com/wp-content/uploads/Courses/FractureMechanics/FractureMechanicsME524.pdf>

Breakdown of your grade:

HW: 34%

Midterm exam: 22%

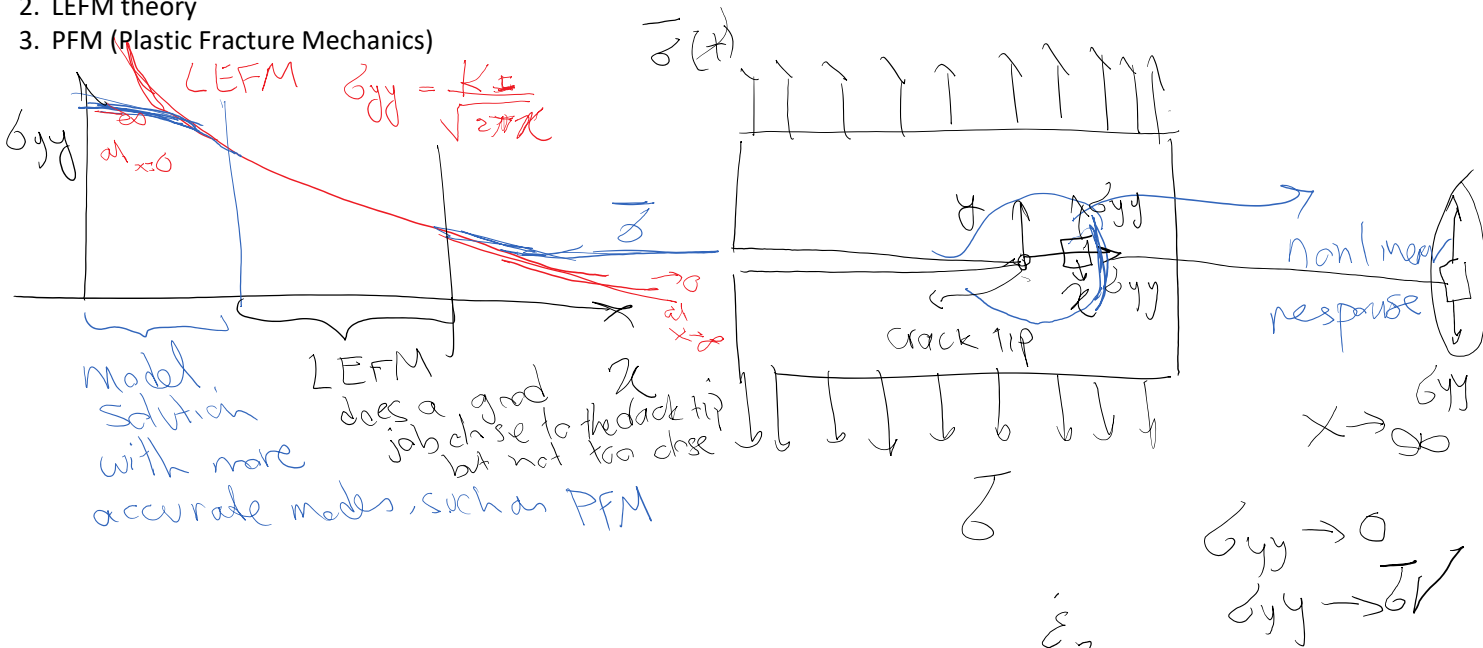
Final exam: 12%

Computational Project: 16% : You will calculate stress intensity factor using a commercial code (Ansys will be used by the instructor)

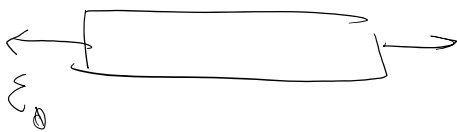
Final Project 16%: Presentation on a fracture mechanics topic that will be communicated with the instructor. Can also do a computational / theoretical / experimental fracture project.

Course outline:

1. Brief introduction to fracture mechanics (ductile and brittle materials and the transition between two failure modes)
2. LEFM theory
3. PFM (Plastic Fracture Mechanics)

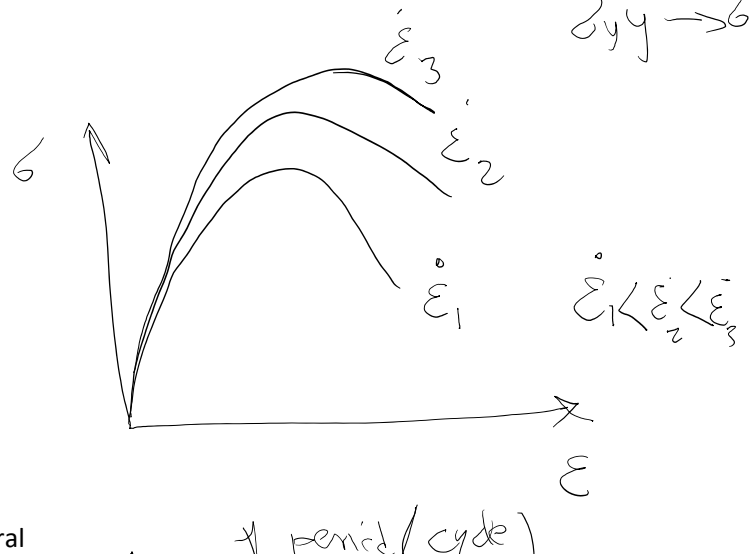


4. Dynamic fracture mechanics and rate effects



Pulling the ends of a bar with different speeds.

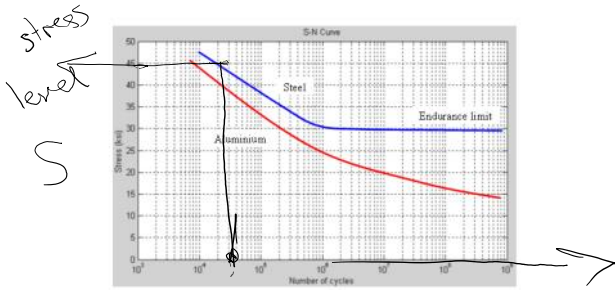
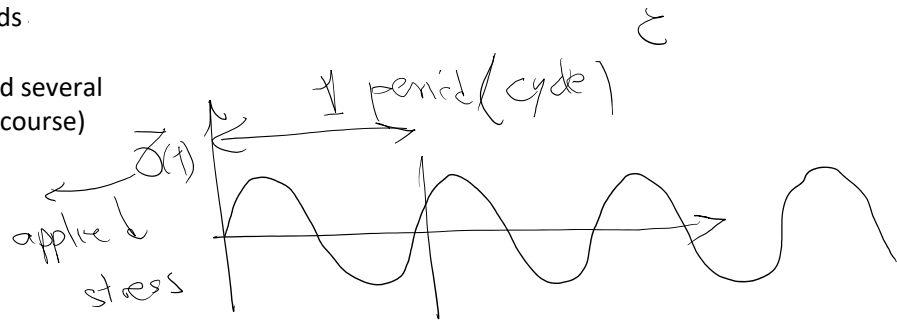
We will also look at dynamic LEFM theory and several



Pulling the ends of a bar with different speeds

We will also look at dynamic LEFM theory and several rate dependent models (near the end of the course)

5. Fatigue

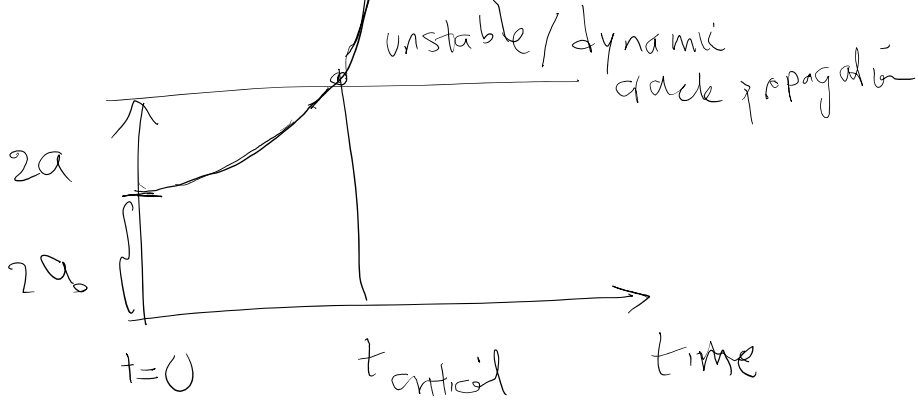
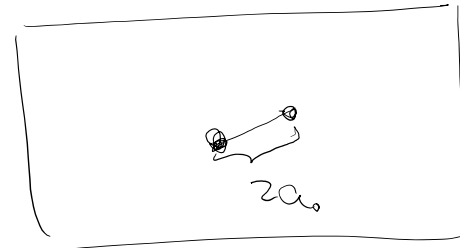
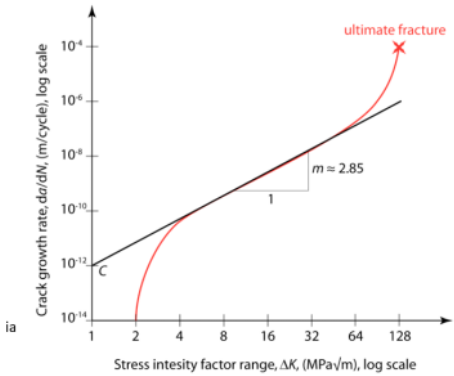


older approach

of cycles
N

More modern approach for modeling fatigue:

We will allow the material to have cracks and model the progress (elongation) of the crack as the number of cycles increase

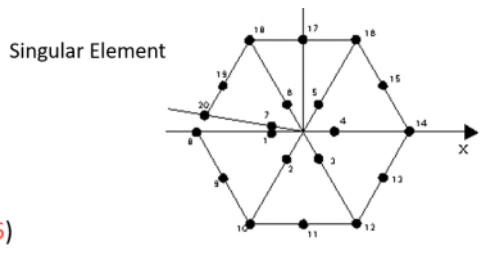


6. Computational Fracture Mechanics

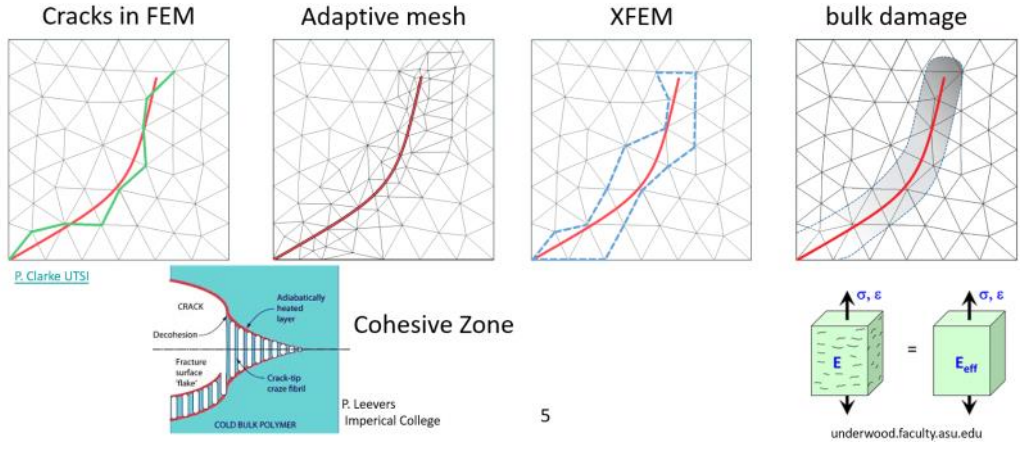
Learn how to extract important fracture mechanics parameters (for example stress intensity factor) from finite element (or other numerical methods') solutions.

Computational fracture mechanics

- FEM aspects:
 - Isoparametric singular elements
 - Calculation of LEFM/EPFM Integrals
 - Adaptive meshing, XFEM



- Cohesive crack model (Hillerborg, 1976)
- Continuum Damage Mechanics
 - size effect (Bazant)



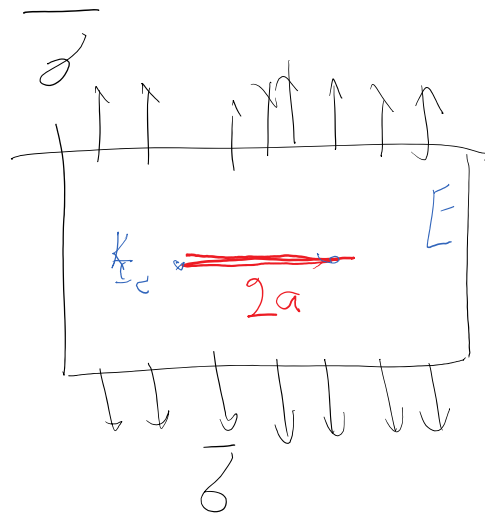
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Today's material

Some background and ductile vs. brittle fracture

Three main problems are encountered in fracture mechanics:

- Model parameters:
- ① Applied/Design loads $\bar{\sigma}$
 - ② Material properties
 - E : elastic modulus
 - K_{IC} : fracture toughness
 - ③ Defect geometry (e.g. crack size)



In design / analysis problems we generally have 2 of these and want to obtain the third one.

- 1 and 2 given (load and material properties are known) and want to find 3, meaning that what crack length is safe.

- b. 1, 3 are given (load and crack length are known) -> what material is needed to withstand the given load. This may not always have a reasonable solution / the original design space may not be reasonable.
- c. 2, 3 are given (material and crack size), want to find the safe design load.
-

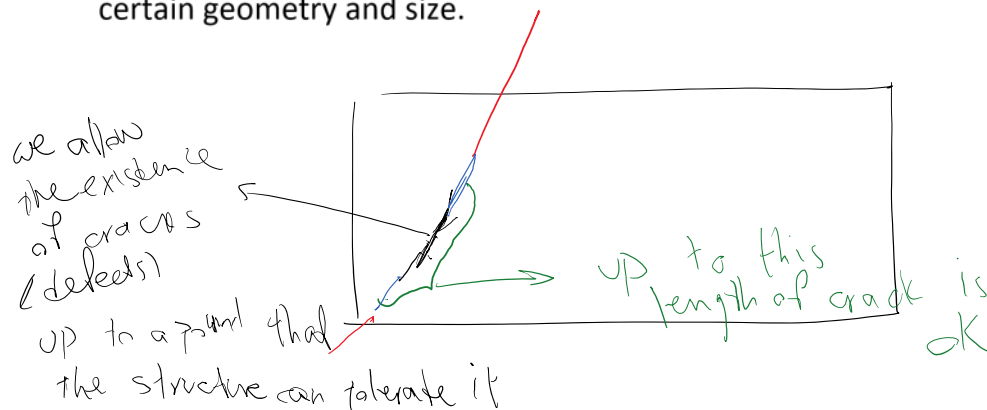
Design philosophies

- Safe life

The component is considered to be free of defects after fabrication and is designed to remain defect-free during service and withstand the maximum static or dynamic working stresses for a certain period of time. If flaws, cracks, or similar damages are visited during service, the component should be discarded immediately.

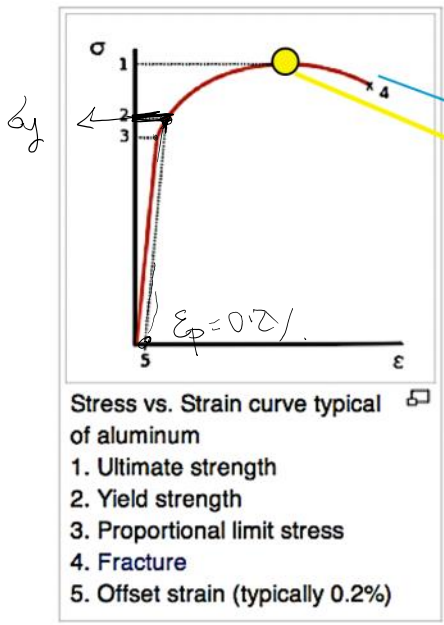
- Damage tolerance

The component is designed to withstand the maximum static or dynamic working stresses for a certain period of time even in presence of flaws, cracks, or similar damages of certain geometry and size.

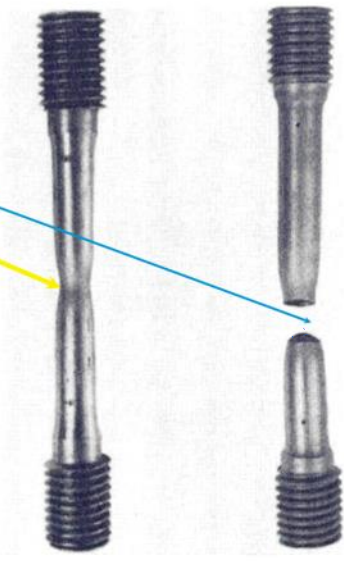


Ductile vs. brittle fracture

Starting point for this discussion:

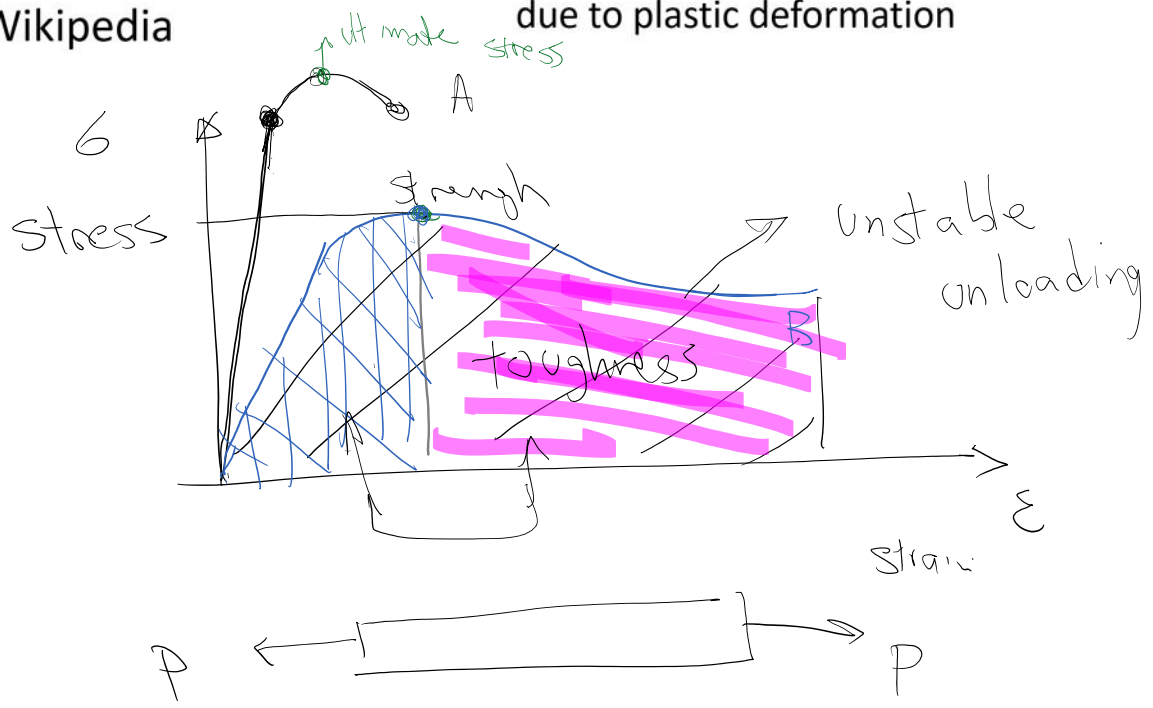


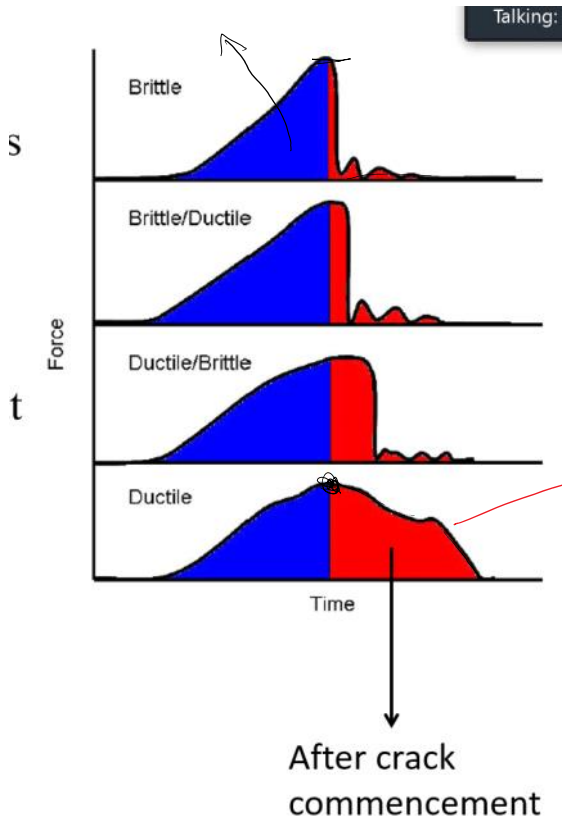
fracture



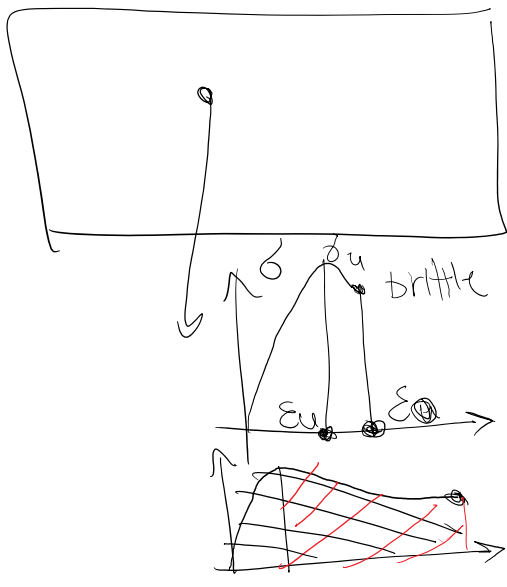
necking=decrease of cross-sectional area due to plastic deformation

Wikipedia

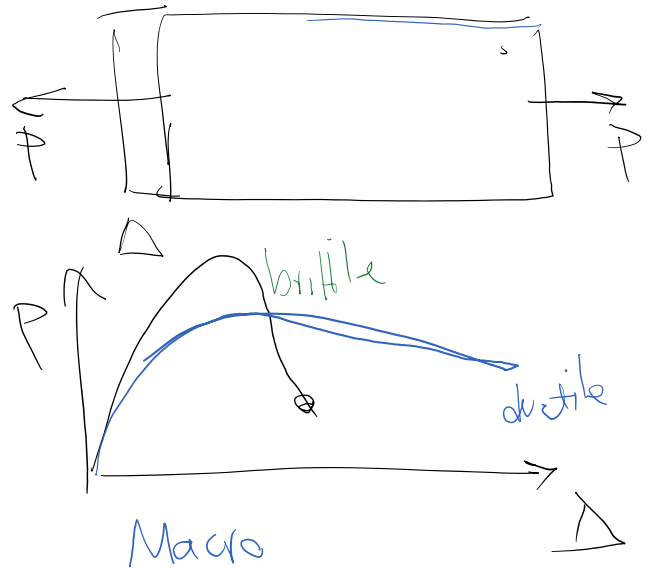




Ductile vs. Brittle is defined in:
 Micro vs. macro scale.
 blk vs. interfacial models

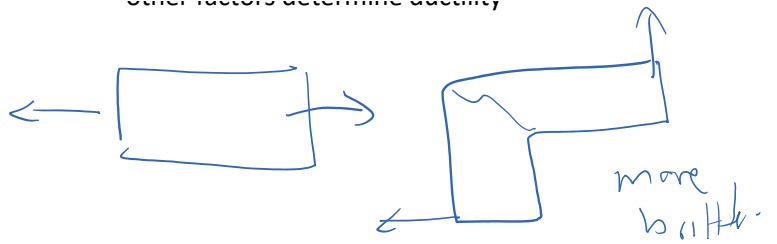


$\epsilon - \sigma$
 macro level



At the macroscale, the constitutive equation of the material, e.g. how brittle it is, and the geometry, plus other factors determine ductility

Other factors determine ductility

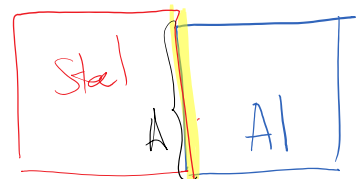
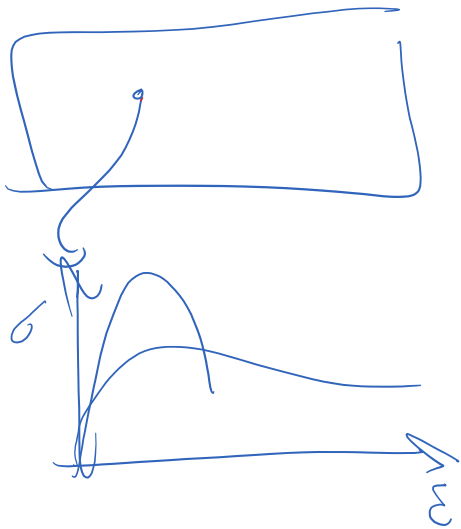


Micro scale

Bulk

vs.

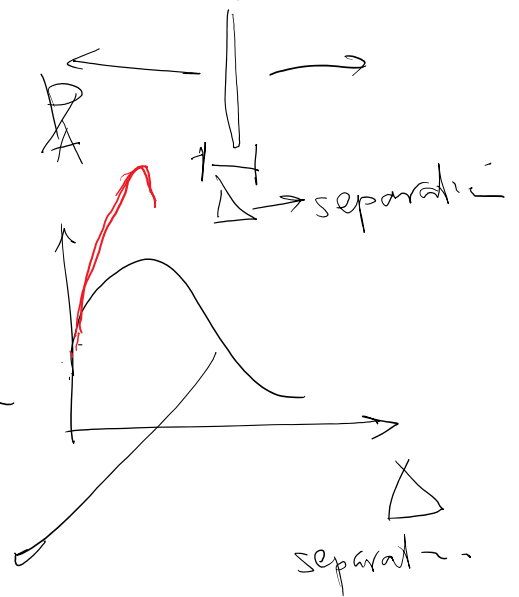
Interface



interface

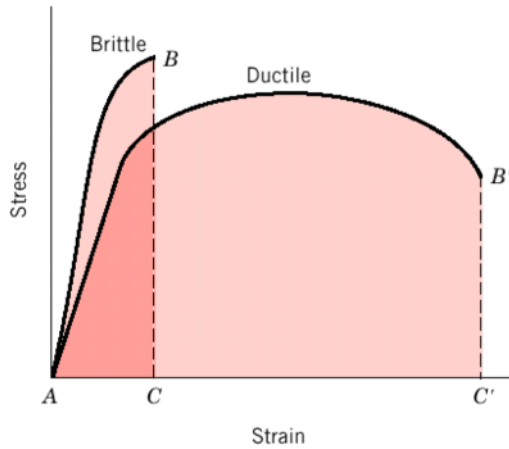
trac_n = $\frac{t}{A}$

Normal traction



Traction-Separation Relation (TSR)

- **Ductile materials** - extensive plastic deformation and energy absorption (“toughness”) before fracture
- **Brittle materials** - little plastic deformation and low energy absorption before fracture

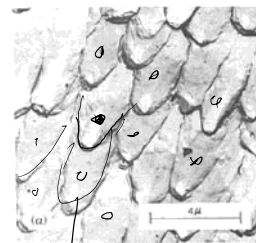
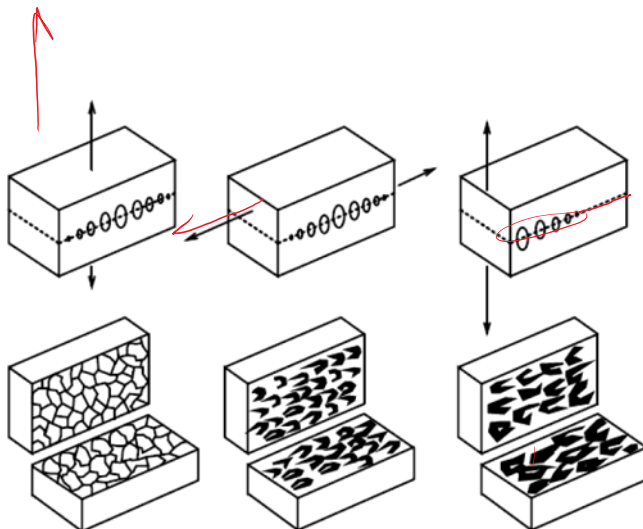
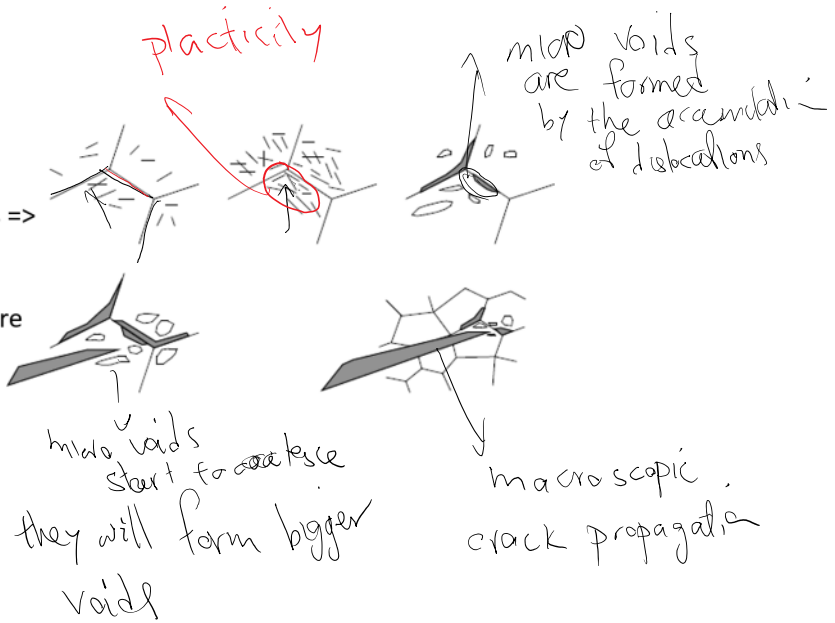


How does ductile fracture happen?

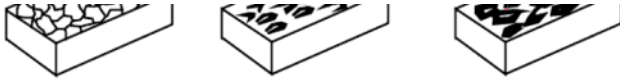
Shearing

- Applied stress =>
- Dislocation generation and motion =>
- Dislocations coalesce at grain boundaries =>
- Forming voids =>
- Voids grow to form macroscopic cracks
- Macroscopic crack growth lead to fracture

Plastic deformation (ductile material)



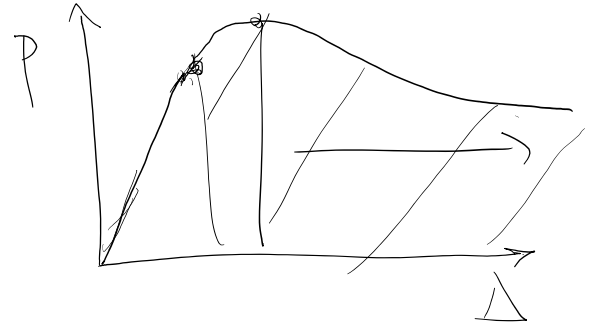
conic fracture patterns on the surface of ductile fracture



On the surface of ductile fracture
ductile fracture surface is
very rough

All these processes (dislocation motion, pile-up against grain boundary, micro void formation, ...) contribute to:

1. Rough fracture surface
2. High fracture energy



A common feature of ductile fracture is ease of motion of dislocations

